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Printed Pages : 3

TCS301

(Following Paper ID and Roll No. to be filled in your Answer Book)

PAPER ID : 1064

Roll No.

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B.Tech**(SEM III) ODD SEMESTER THEORY EXAMINATION 2009-10
DISCRETE STRUCTURE**

Time : 3 Hours]

[Total Marks : 100

Note : Attempt all questions.**1** Attempt any **four** parts of the following : **5×4=20**

(a) Show that $(R \subseteq S) \wedge (S \subset Q) \Rightarrow R \subset Q$. Is it correct to replace $R \subset Q$ by $R \subseteq QP$.. Explain your answer.

(b) Let $N = \{0, 1, 2, 3, \dots\}$. Define functions f, g and h from set N to N by $f(n) = n+1$,

$$g(n) = 2n, h(n) = \begin{cases} 0 & \text{if } n \text{ is even} \\ 1 & \text{if } n \text{ is odd} \end{cases}$$

Compute $go(fog)oh$.Is the function h is invertible ?Is the function f is on to ?

(c) Given a covering of the set $S = \{A_1, A_2, \dots, A_n\}$, show how you can write a compatibility relation which defines this covering.



- (d) Let $f: X \rightarrow Y$ and $g: Y \rightarrow X$. Prove that the function g is equal to f^{-1} only if $gof = I_x$ and $fog = I_y$.
- (e) Show that the predicate "x is prime" is primitive recursive.
- (f) Show that $n^3 + 2n$ is divisible by 3.

2 Attempt any **four** parts of the following : **5×4**

- (a) If G is a group in which $(ab)^i = a^i b^i$ for three consecutive integers i and any a, b in G , show that G is abelian.
- (b) Show that the intersection of any two congruence relations on a set is also a congruence relation.
- (c) Show that the relation of isomorphism is an equivalence relation.
- (d) Show that every finite semigroup has an idempotent.
- (e) Show that for any commutative monoid $\langle M, * \rangle$, the set of idempotent elements of M forms a submonoid.
- (f) Write about cosets and permutation groups.

3 Attempt any **two** parts of the following : **10×2=20**

- (a) Give an example of a set X such that $\langle \rho(X), \subseteq \rangle$ is a totally ordered set.
- (b) Prove that a n variable boolean function having products of all maxterm is zero.
- (c) (i) Define Binary search tree. Show the insertion of an element in an existing binary search tree.
- (ii) Prove that a tree with n vertices will have $n-1$ edges.

4 Attempt any **two** of the following parts : **10×2**

- (a) (i) Write the following statement in symbolic form. "If either Ram takes Maths or Shyam takes Science, then Hari will take Biology".
- (ii) Construct the truth table for $(P \rightarrow Q) \wedge (Q \rightarrow P)$.
- (b) Obtain formulas having the simplest possible form which are equivalent to formulas :
- (i) $P \vee (\neg P \vee (Q \wedge \neg Q))$.
- (ii) $(P \wedge (Q \wedge S)) \vee (\neg P \wedge (Q \wedge S))$.
- (c) Show that $\neg P(a, b)$ follows logically from (x) $(P(x, y) \rightarrow w(x, y))$ and $\neg W(a, b)$.

5 Attempt any **two** of the following parts : **10×2**

- (a) (i) Solve the recurrence relation $dn = 2dn - 1 - dn - 2$.
- (ii) Write about linked list representation of graphs.
- (b) Show that if G be a graph of n vertices and m edges then G has Hamiltonian circuit if $m \geq \frac{1}{2}(n^2 - 3n + 6)$.
- (c) (i) Prove that a tree of connected graph has no circuit.
- (ii) Define Euler graph. Give a suitable example for it.